

II B. Tech I Semester Supplementary Examinations, May - 2018
MATHEMATICAL FOUNDATION OF COMPUTER SCIENCE
 (Com to CSE & IT)

Time: 3 hours

Max. Marks: 70

- Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)
 2. Answer **ALL** the question in **Part-A**
 3. Answer any **FOUR** Questions from **Part-B**

PART -A

1. a) Construct truth table for the compound predicate: $p \rightarrow (\neg q \wedge r)$ (2M)
- b) Draw the Hasse diagram for the power set $(P(S), \leq)$, where $S = \{1, 2, 3\}$. (3M)
- c) Write a note on \equiv operator in modular arithmetic. (2M)
- d) How many ways are there to arrange the letters of the word ENGINEERING? (2M)
- e) Solve the following recurrence relation using generating functions: $a_n - 6a_{n-1} = 0$ for $n \geq 1$ and $a_0 = 1$. (3M)
- f) A complete binary tree has 125 edges. How many vertices does it have? (2M)

PART -B

2. a) Show that the following statement is a tautology: (7M)
 $(\sim P \wedge (P \rightarrow Q)) \rightarrow (\sim Q)$
- b) Using automatic theorem proving, show that: (7M)
 $(P \vee Q) \wedge (Q \rightarrow R) \wedge (P \rightarrow M) = (R \vee M)$
3. a) Verify the following relation R on $X = \{1, 2, 3, 4\}$ is an equivalence relation or not? Given $R = \{(1, 1), (1, 4), (4, 1), (2, 2), (2, 3), (3, 4), (3, 3), (3, 2), (4, 3), (4, 4)\}$. (7M)
- b) Given below the relation matrix, M_R of a relation R on the set $\{a, b, c\}$, find the relation matrices of $R^2 = R \circ R$, $R^3 = R \circ R \circ R$. (7M)

$$M_R = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

4. a) Explain different tests for primality. (7M)
- b) Prove that $G = \{-1, 1, i, -i\}$ is an Abelian group under multiplication. (7M)
5. a) What are the applications of Binomial and Multinomial coefficients? (7M)
- b) In how many ways can you select at least one king, if you choose five cards from a Deck of 52 cards? (7M)
6. a) Verify by mathematical induction that $a_n = A_1 n + A_2$ is a solution to $a_n = d a_{n/d} + e$ where $n = d^k$. (7M)
- b) Write about partial fraction decomposition. (7M)
7. a) What is a cut vertex, cut set and bridge? Explain with suitable examples. (7M)
- b) Show that the maximum number of edges in a complete bipartiate graphs with n vertices is $n^2/4$. (7M)

